

Inverse Toon Shading: Interactive Normal Field Modeling with Isophotes

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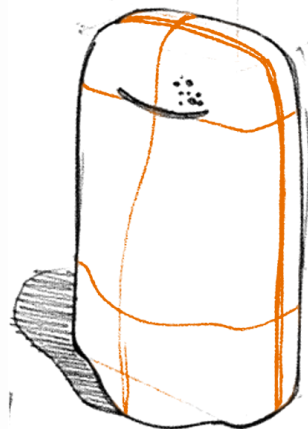
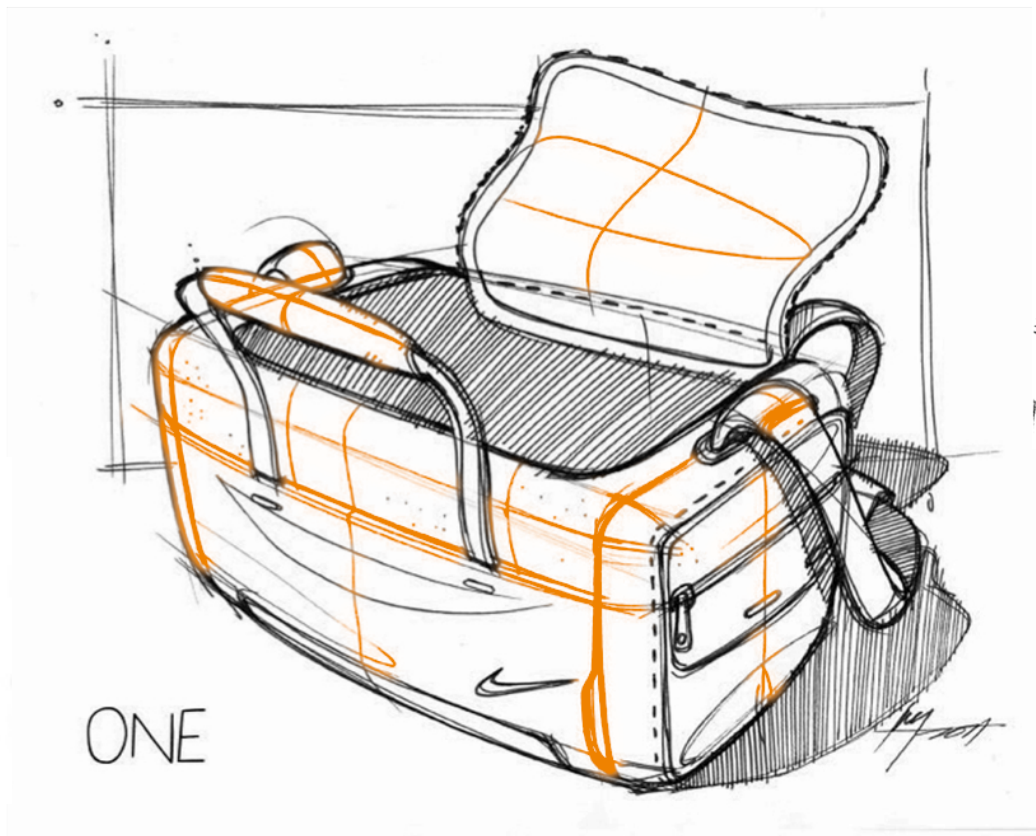
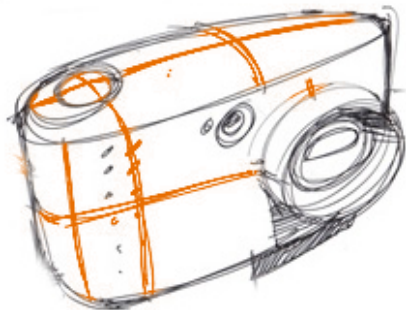
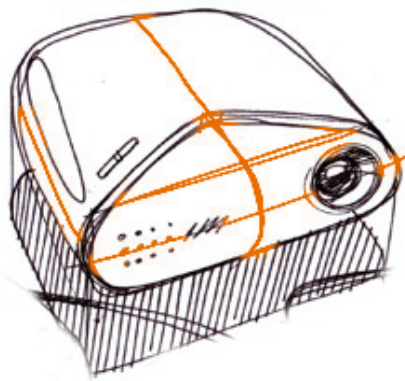
Presentation Renderings



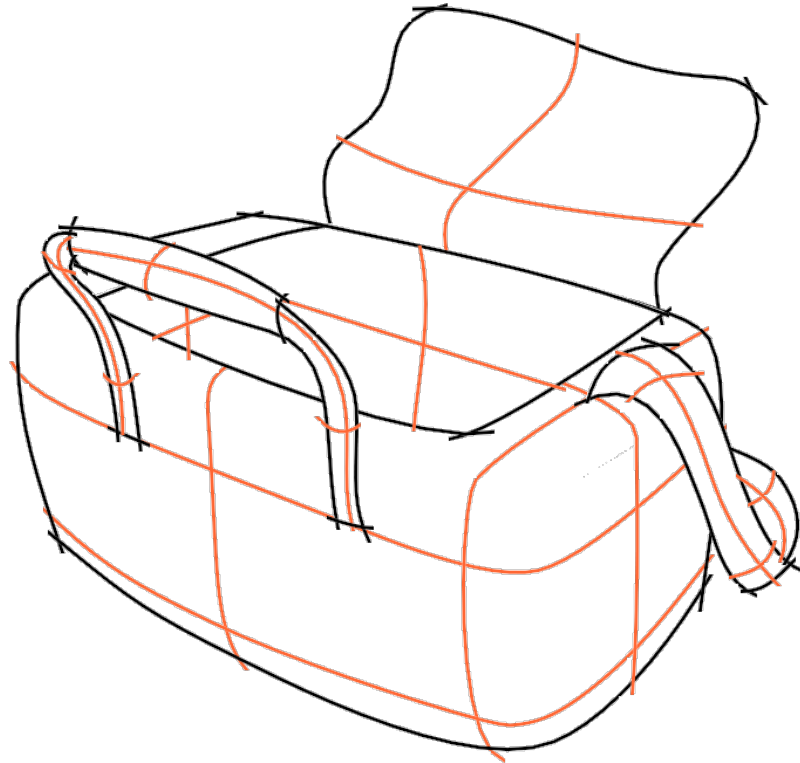
Presentation Renderings



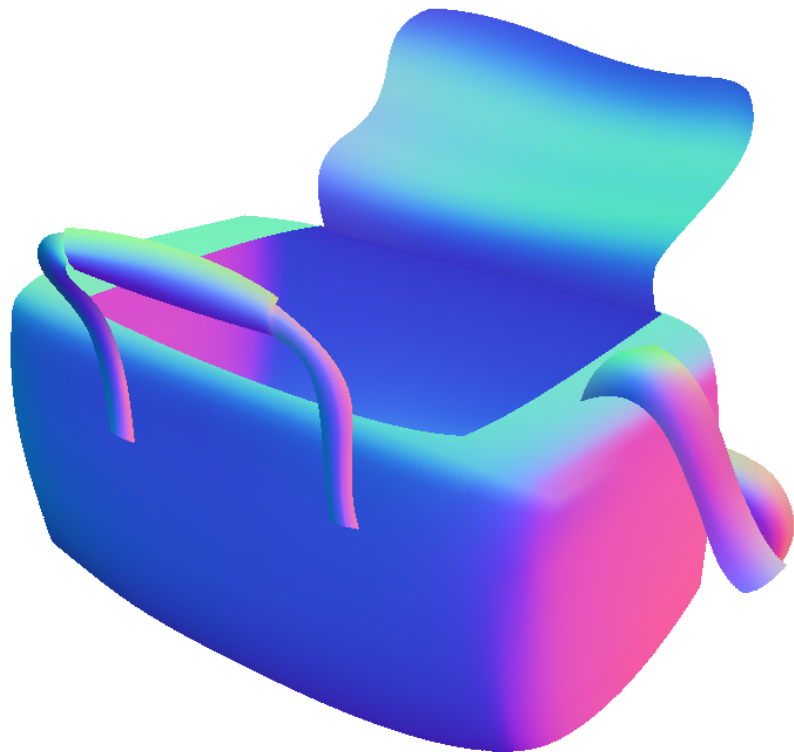
Cross-section sketch >



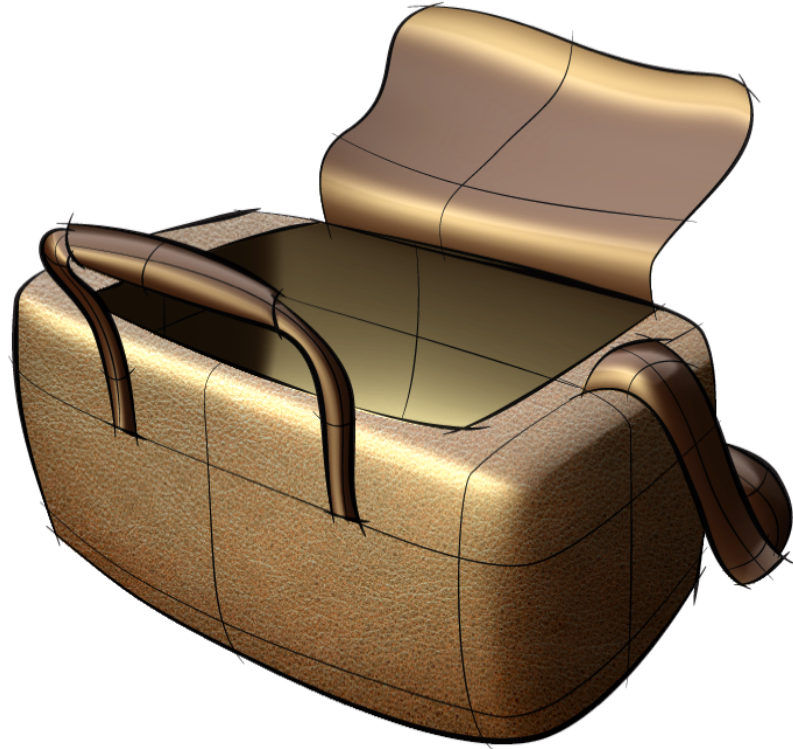
Cross-section sketch >



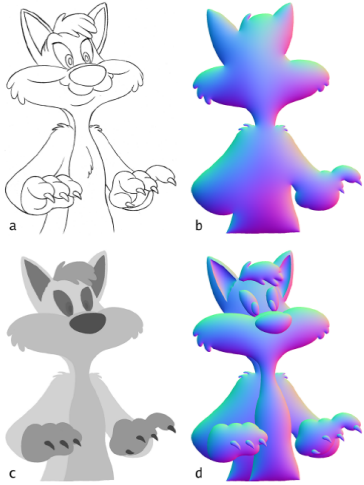
3D normals >



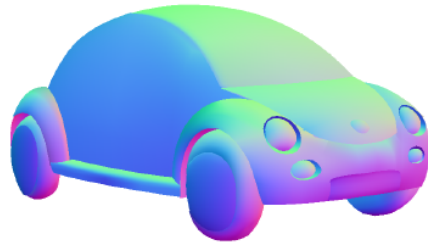
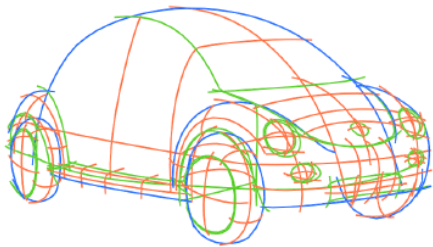
Presentation Renderings!



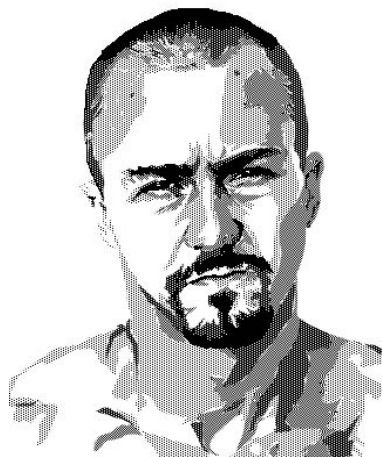
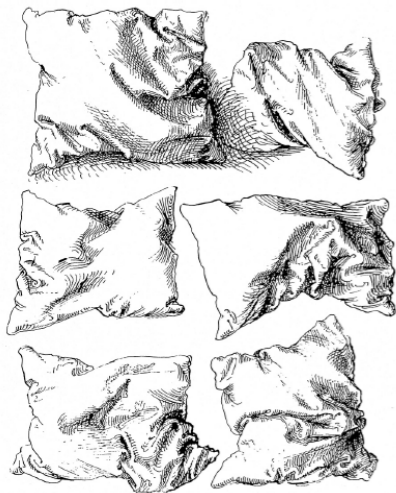
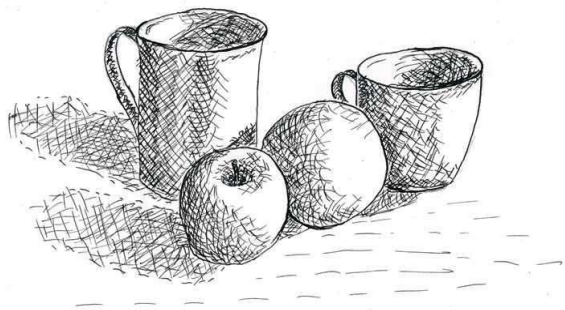
Related Work



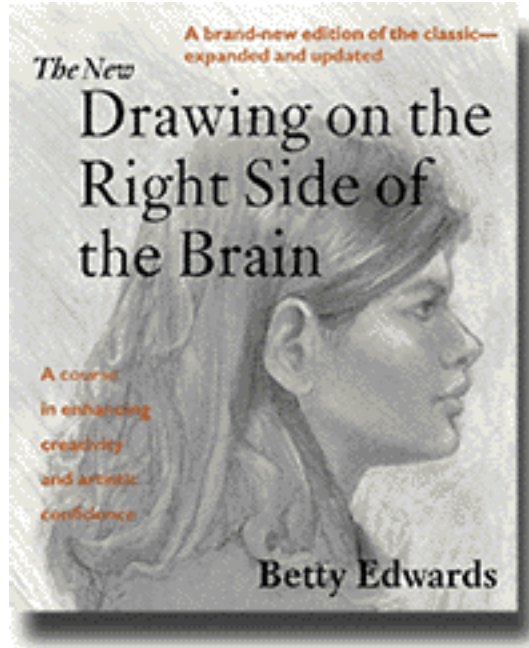
Lumo
NPAR 2002.



CrossShade
SIGGRAPH 2012.



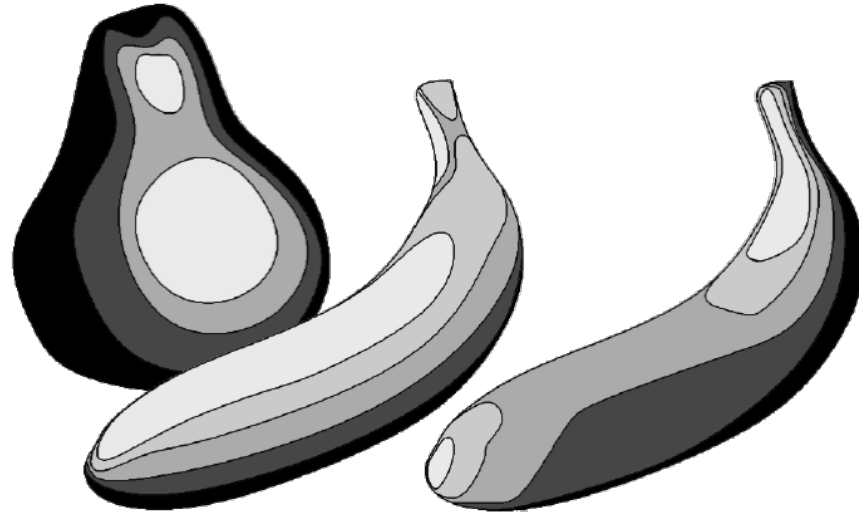
Blocking-in light and shade



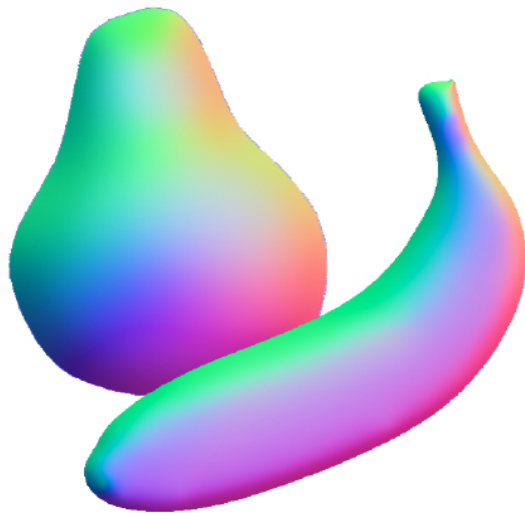
Design Principles

- Sketched curves are descriptive of 3D: 2D shape \approx 3D shape.
- Surface is artistically imagined by massing: local primitives.

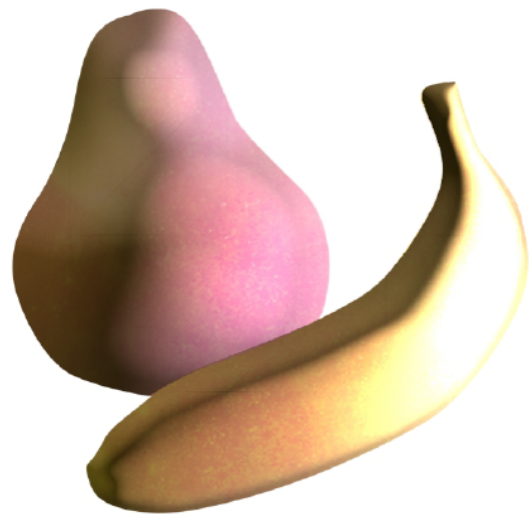
Inverse Toon Shading



Inverse Toon Shading



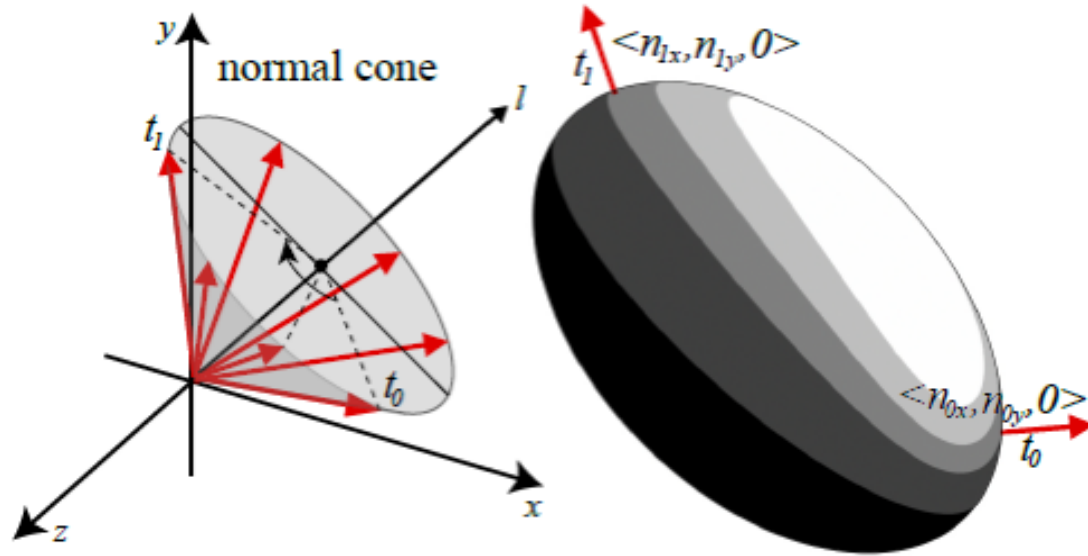
Inverse Toon Shading



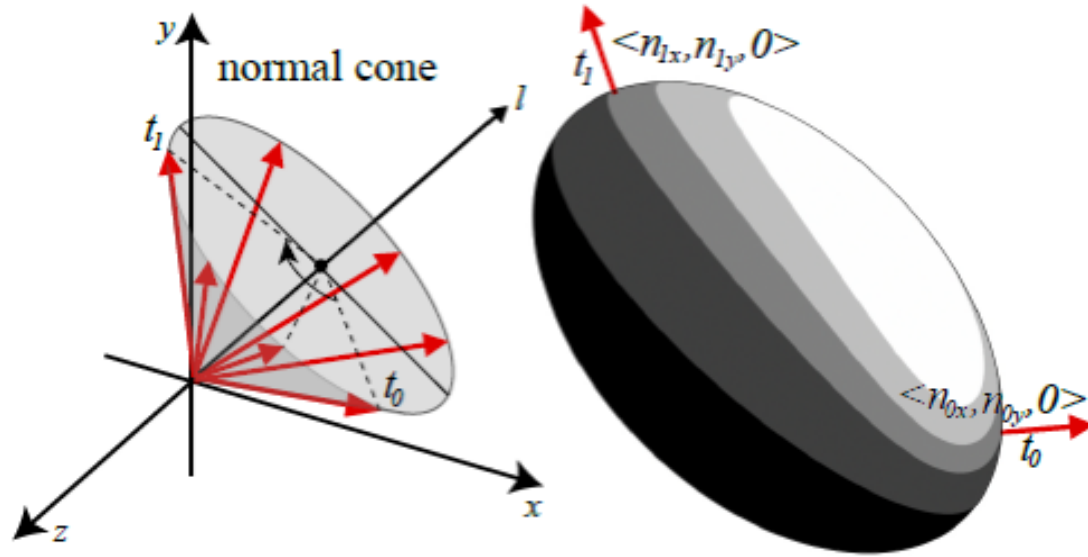
Assumptions

- Smooth 3D shapes (tangent continuity).
- Directional front lighting.
- Diffuse Lambertian Reflection with Specular hot-spots.
- No cast shadows.
- No internal occluding contours.

Light and Value

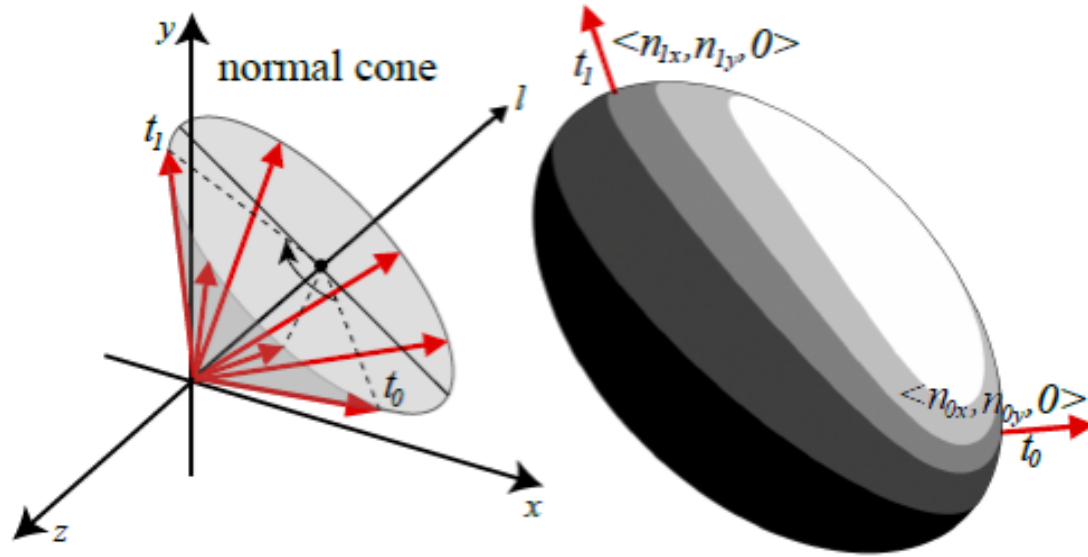


Light and Value



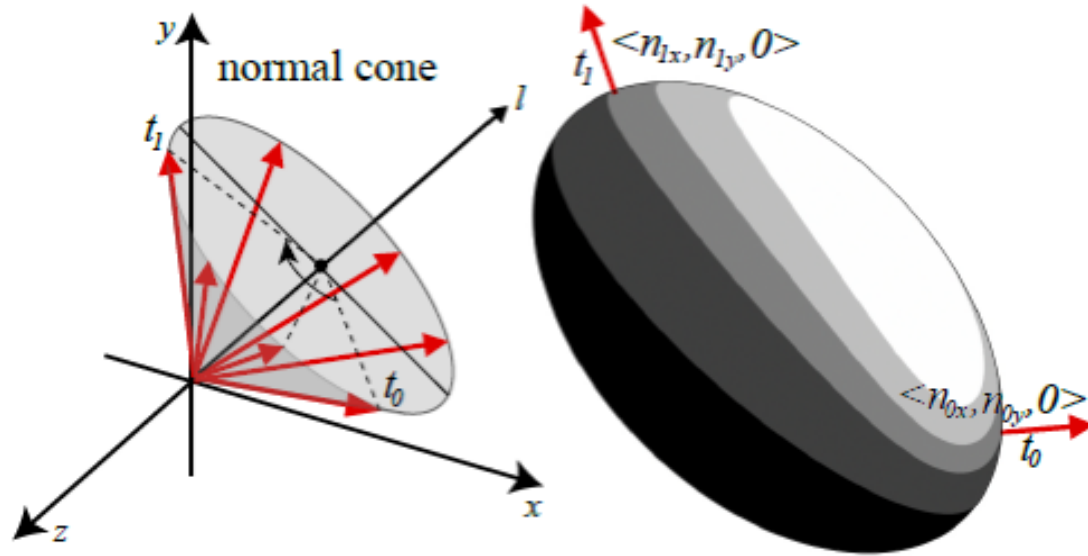
$$l = \langle n_{0x} + n_{1x}, n_{0y} + n_{1y}, z \rangle$$

Light and Value

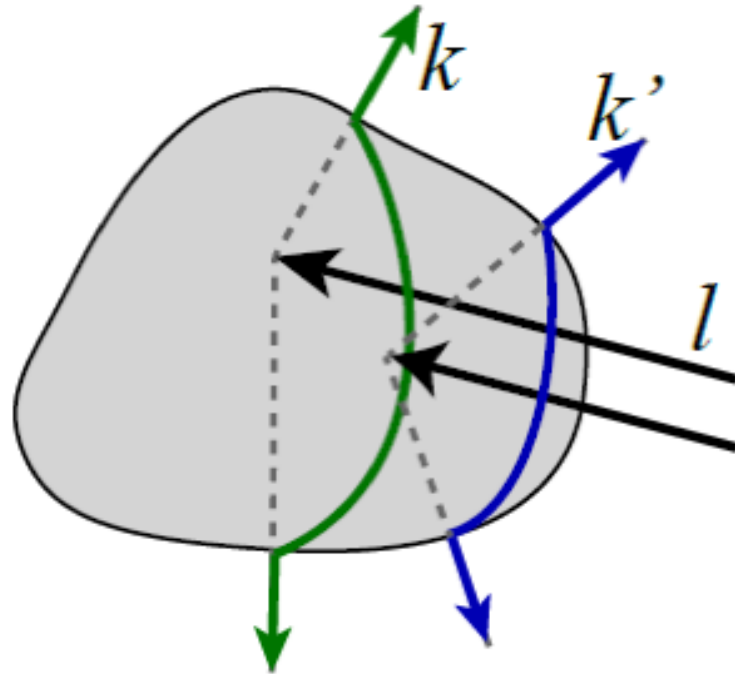
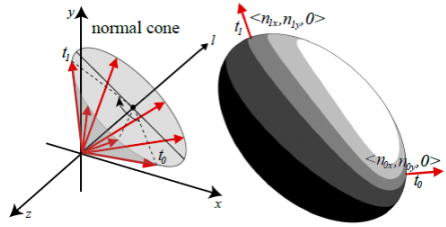


$$l = \langle n_{0x} + n_{1x}, n_{0y} + n_{1y}, z \rangle$$
$$z = \pm \sqrt{(1 + n_0 \cdot n_1)^2 / k^2 - 2(1 + n_0 \cdot n_1)}.$$

Light and Value



Light and Value



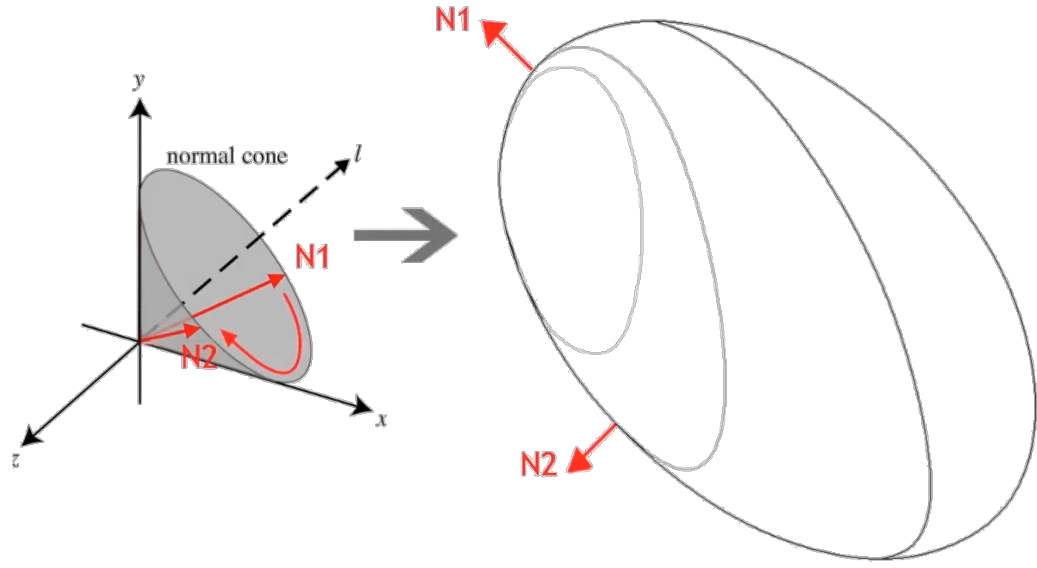
Workflow

Workflow

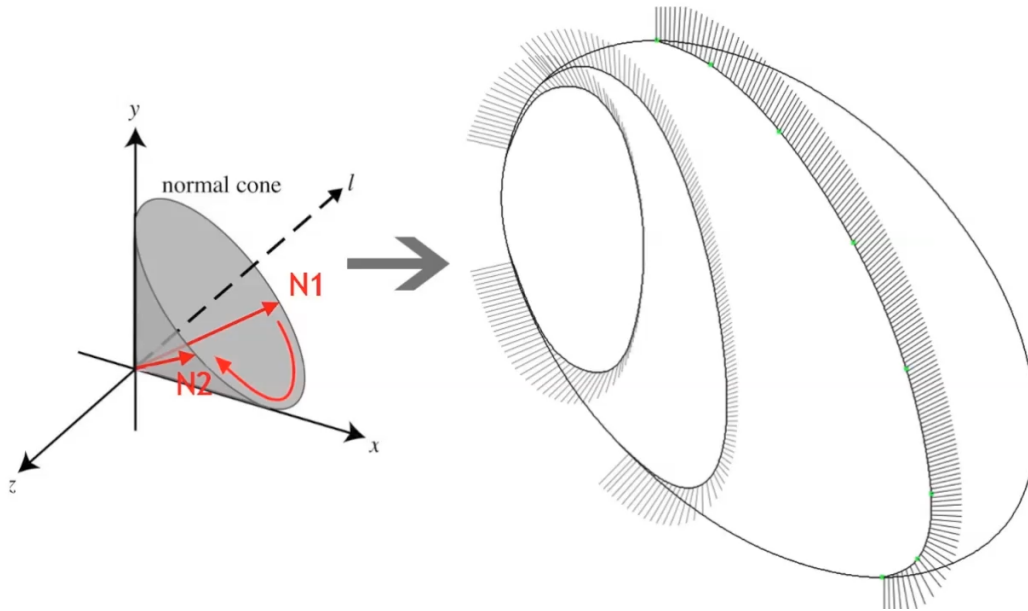
Well defined normals

- Silhouettes and internal contours.
- Intersecting isophotes from different lights.
- Specular hot-spots.

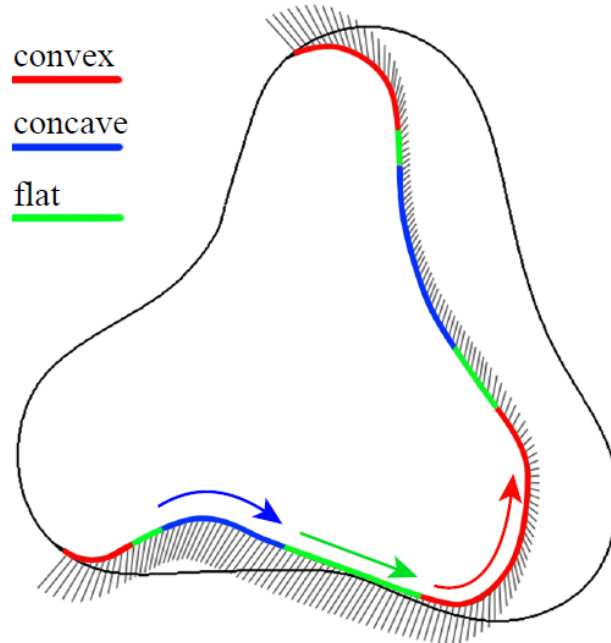
2D arc-length interpolation



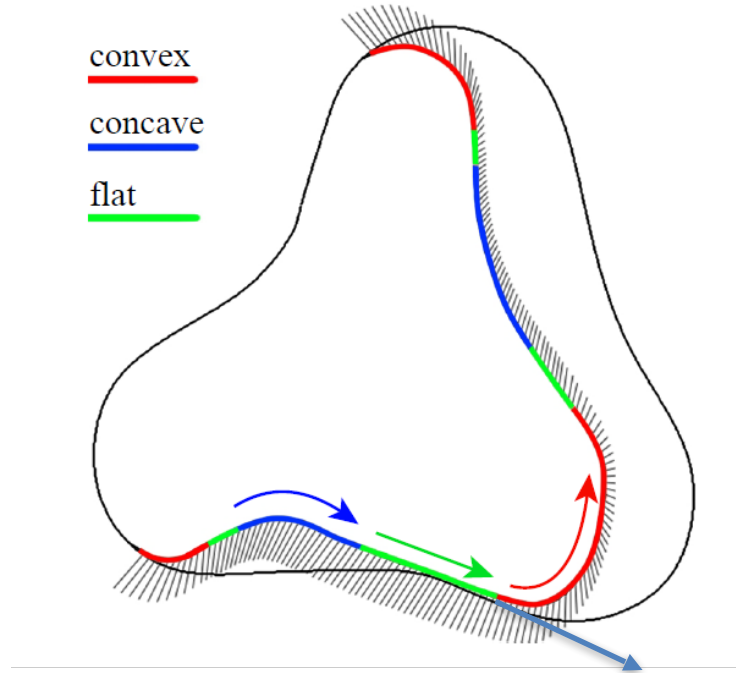
2D arc-length interpolation



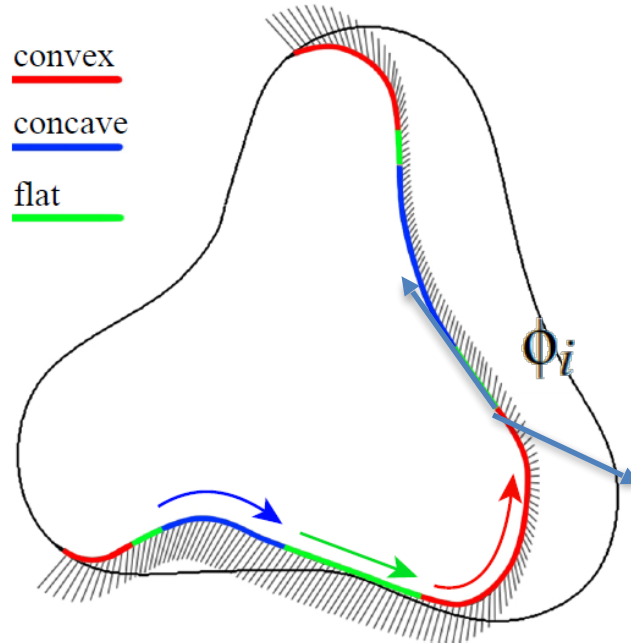
Curvature segmentation



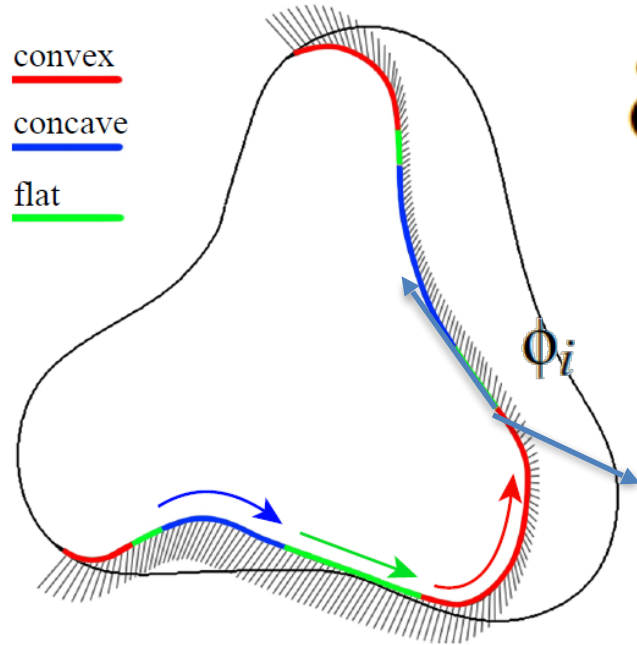
Curvature segmentation



Curvature segmentation



Curvature segmentation



$$\delta t_i = \frac{\phi_i \Delta t}{\sum_0^m \phi_i}$$

Missing Primitives

- Even 3D ellipsoids have complex non-planar 3D isophotes. ☹
- Linear 3D isophote => constant normal line on ruled surface.
- Circular 3D isophote $(0, \cos(a), \sin(a))$ => 3D normal $\frac{\langle x, \cos(a), \sin(a) \rangle}{\sqrt{1+x^2}}$

aspect and tilt angle of 2D ellipse defines 3D transform M to image.

If light l is $l' = M^{-1}l$, $xl'_x + \cos(a)l'_y + \sin(a)l'_z = k\sqrt{1+x^2}$
solve for x !

2D ellipse fitting

Fit a minimal number of 2D ellipses to each convex/concave isophote segment.
Each ellipse segment maps to 4 normal choices (2 tilt directions, and convex/concave).

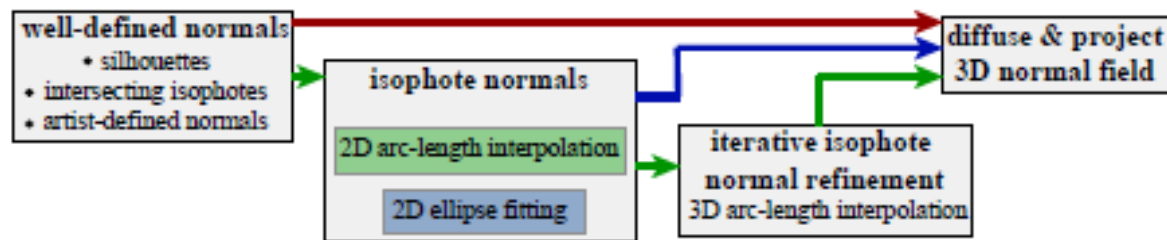
Globally optimize the choices for:

- matching normals at shared point between adjacent segments;
- minimal normal variation within each segment;
- normals that have positive z components;

3D arc-length interpolation

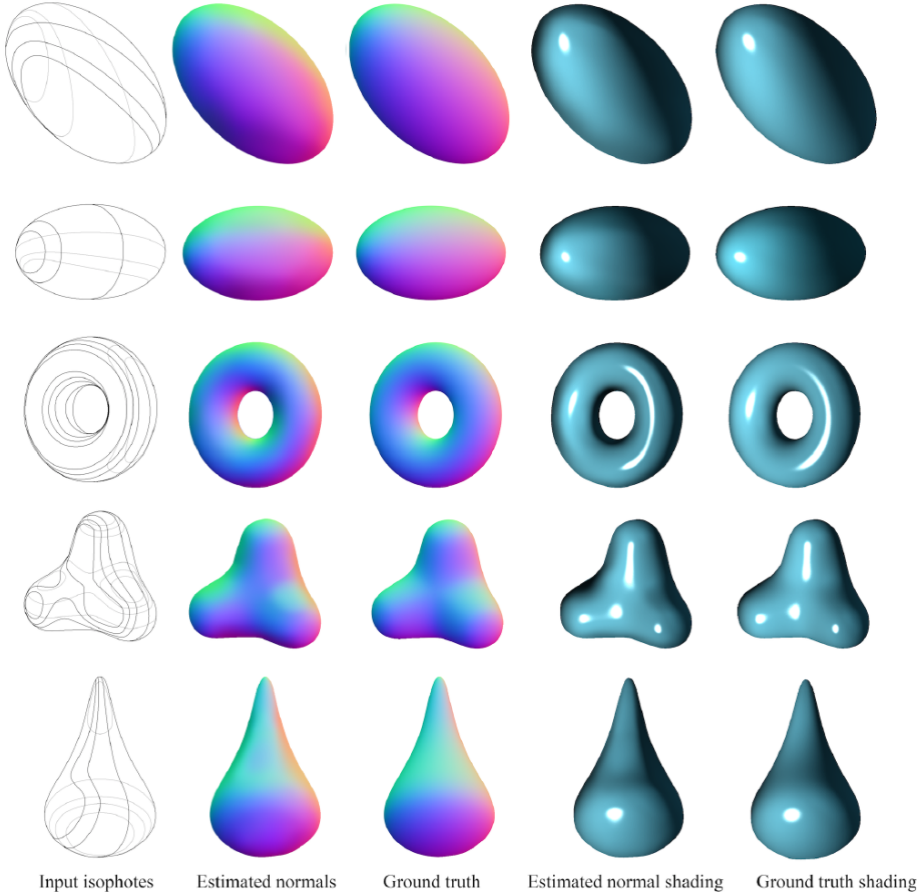
- Estimate 3D isophote tangent $\langle t_x, t_y, t_z \rangle$ from 3D normal $t_z = -\frac{n_x t_x + n_y t_y}{n_z}$.
- Iteratively re-interpolate 3D normal based on 3D arc-length.

Diffuse and Project 3D normals

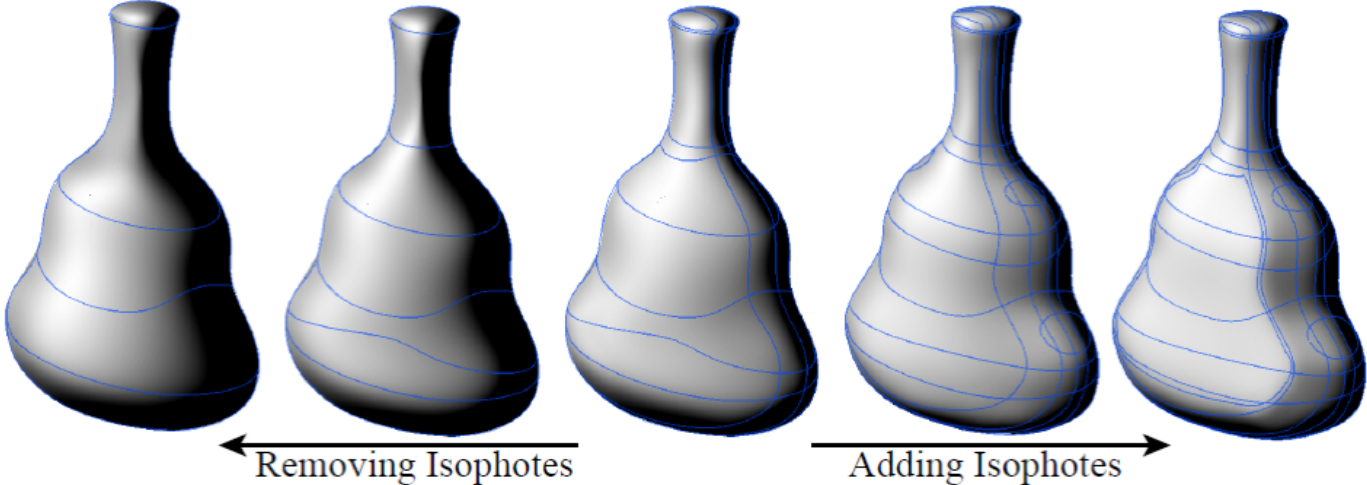


	2d		2d + 3d		ellipse fitting		ellipse + 3d		diffuse only		2d + 3d + diffuse	
	md.	std.	md.	std.	md.	std.	md.	std.	md.	std.	md.	std.
sphere	6.51	4.55	4.94	3.35	4.99	3.4	4.94	3.35	8.85	5.44	4.9	3.24
ellipsoid1	6.33	5.41	5.76	4.11	6.71	6.34	6.6	6.35	8.52	5.5	5.3	3.45
ellipsoid2	6.29	4.05	5.51	3.38	6.28	5.19	5.84	3.81	14.11	14.52	5.46	3.3
torus	7	5.3	6.06	5.09	7.9	12.97	6.27	12.31	7.6	5.05	5.97	4.89
trebol	7.21	9.21	7.04	9.57	8.15	11.63	7.39	9.69	7.7	5.73	6.4	4.63
drop	7.09	7.48	6.1	6.95	6.27	4.92	5.93	4.56	7.27	5.7	5.86	5.1

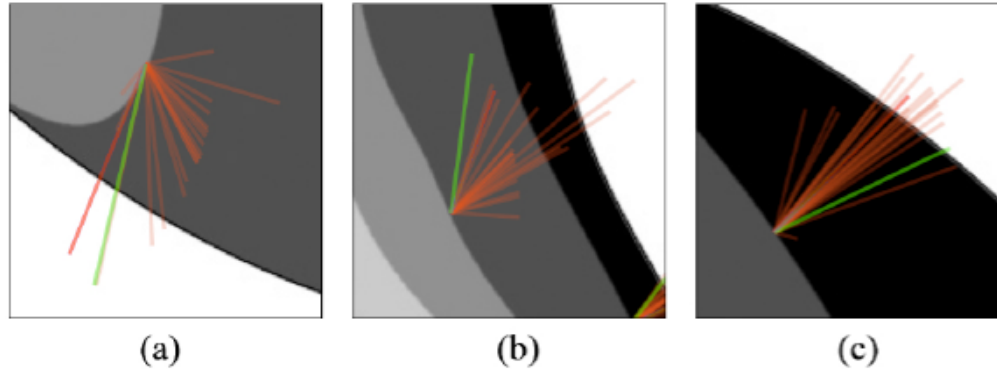
Evaluation



Evaluation

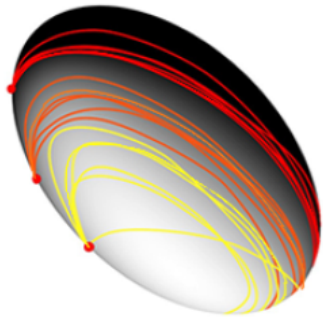
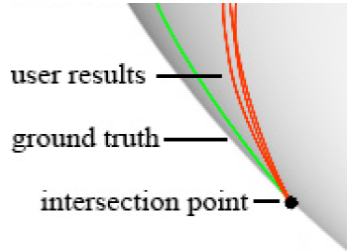


Perceptual Study #1

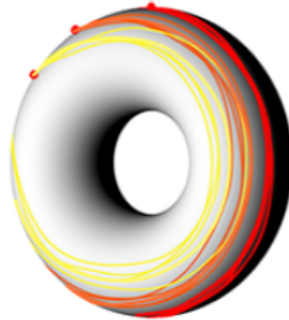


	Pers. intra user	Cons. inter user	Acc. user/GT	Acc. user/GT - outliers	Cons. user/algo	Acc. algo/GT
Complete (constrained movement)						
median	7.1	8.2	16.4	15	14.5	5.6
mean	10.1	14.1	20.2	17.9	15.6	5.8
std. dev.	16.3	17.1	16.8	13.5	13.4	4.2
samples	98	1616	314	299	314	65

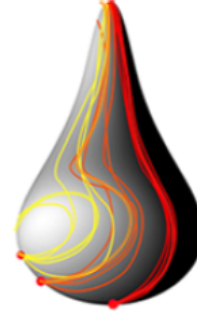
Perceptual Study #2



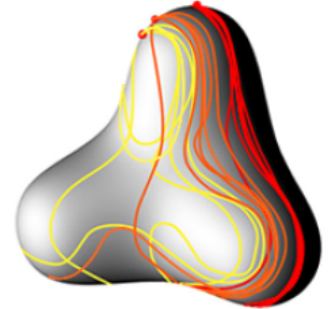
(a)



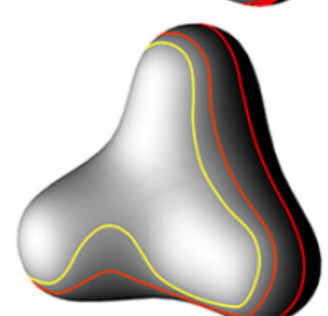
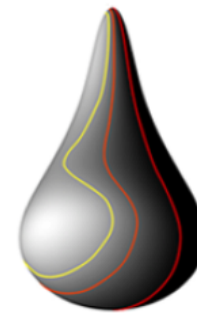
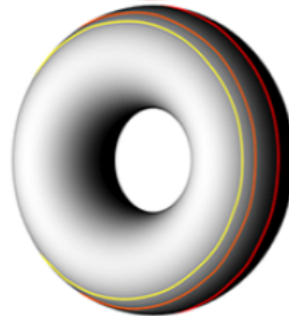
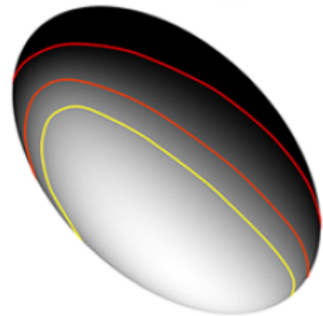
(b)



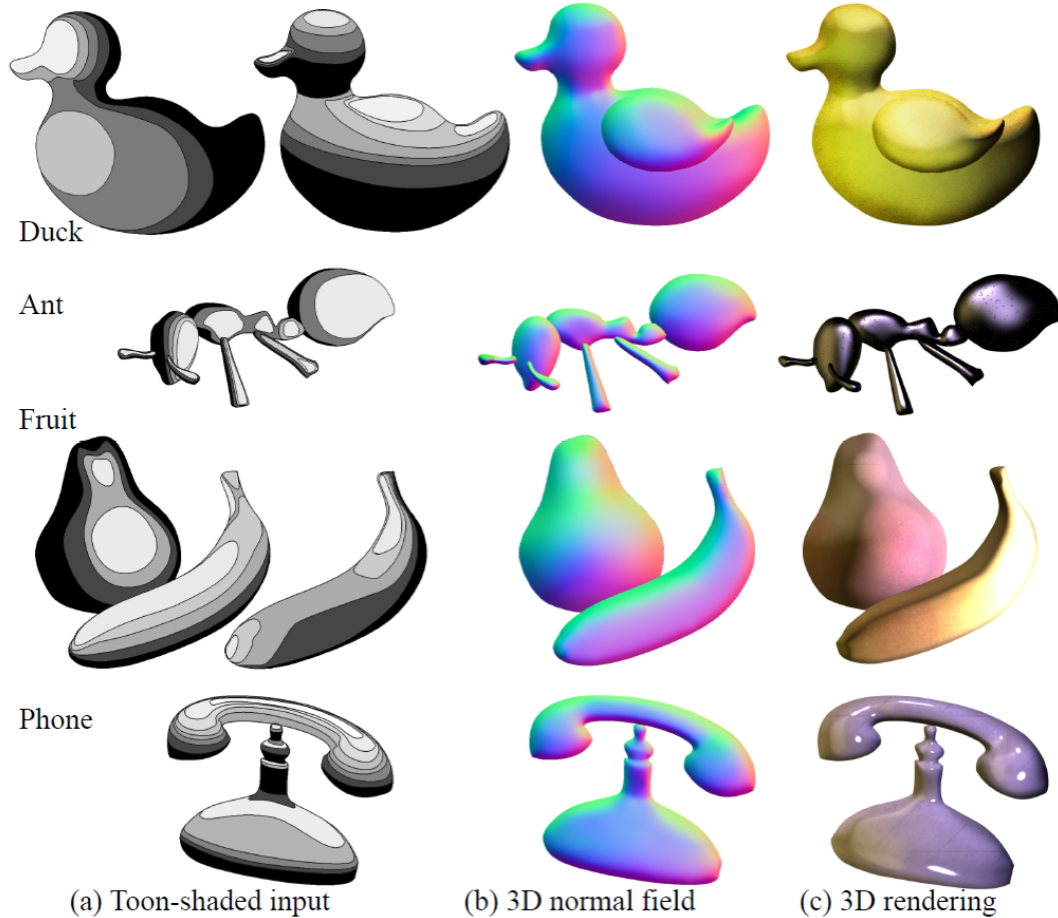
(c)



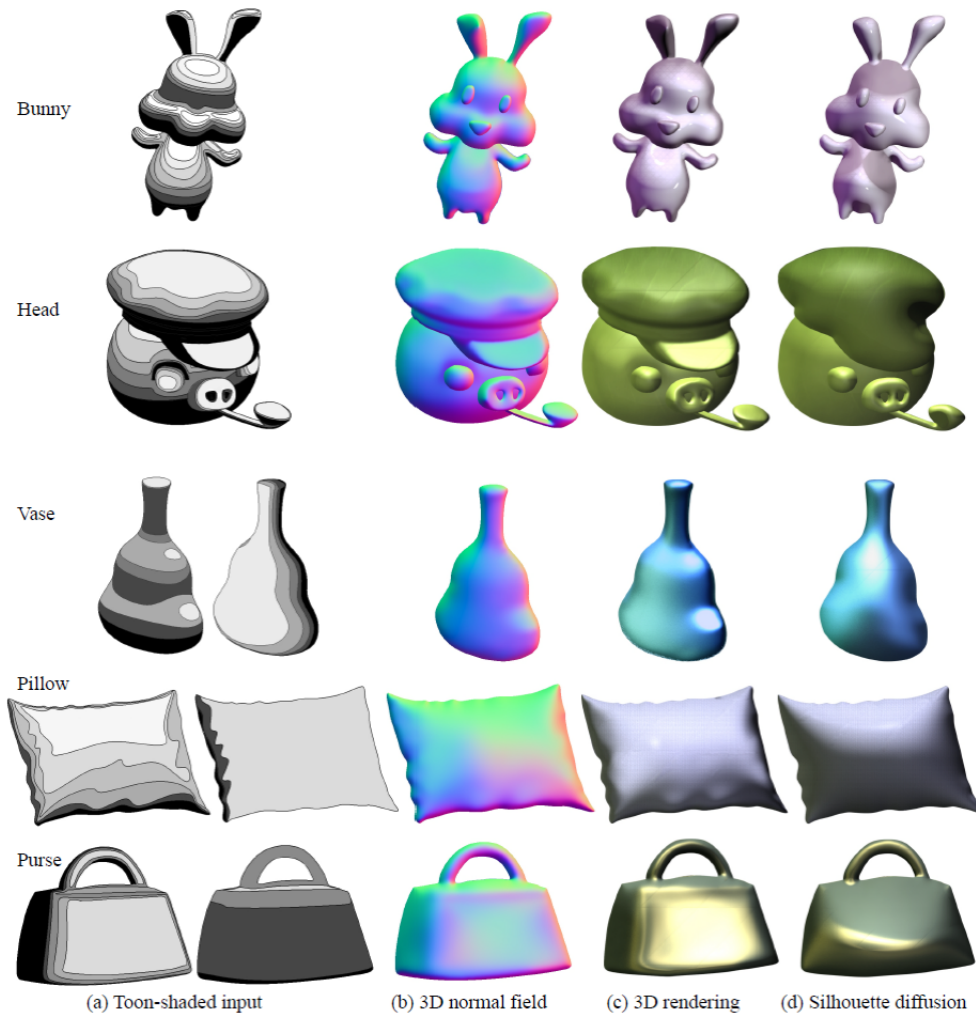
(d)



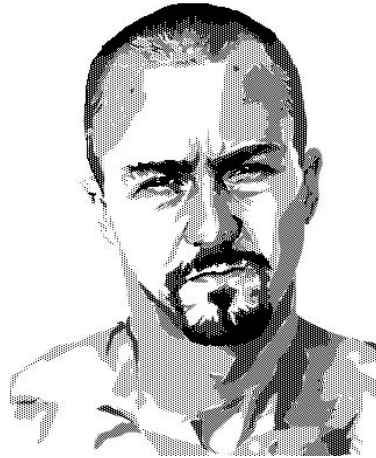
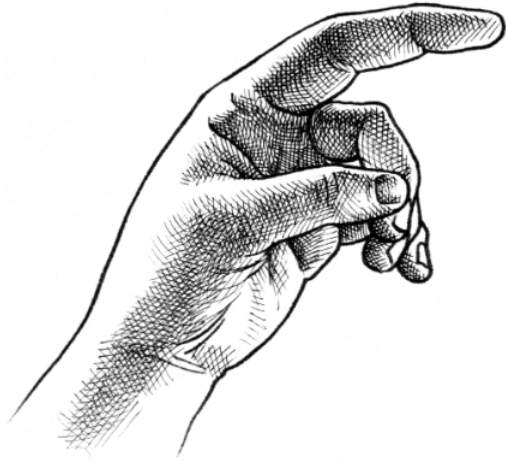
Results



Results



Future work

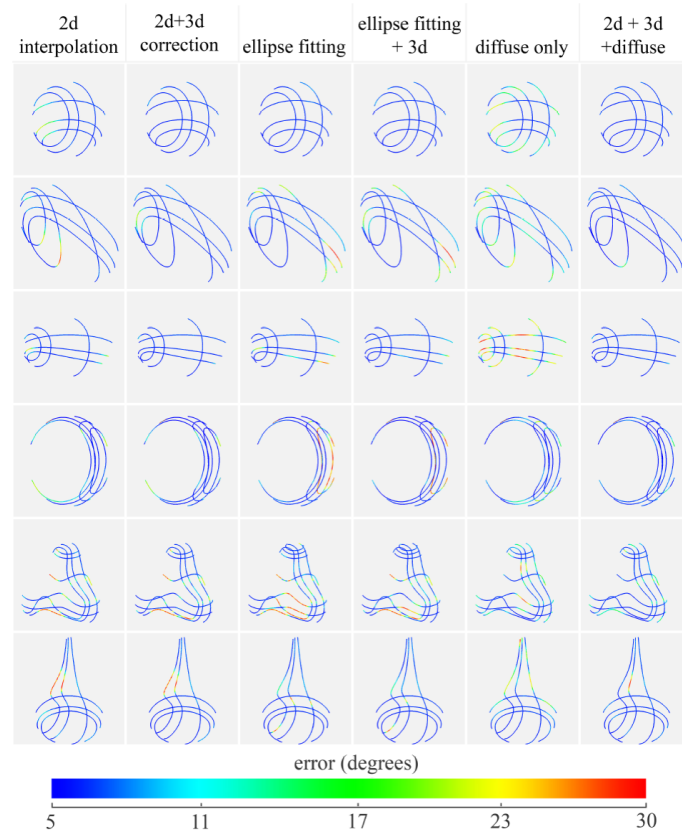


Message

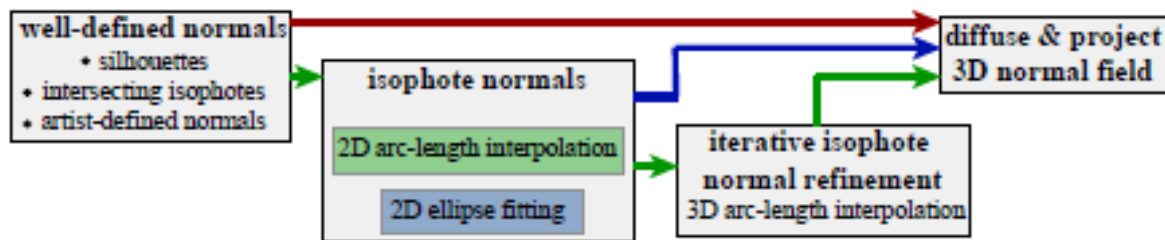
Isophotes can be imagined, drawn and exploited for
3D presentation renderings!

...teşekkür ederim

Diffuse and Project 3D normals



Diffuse and Project 3D normals



	2d		2d + 3d		ellipse fitting		ellipse + 3d		diffuse only		2d + 3d + diffuse	
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